

In the Name of God

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# IRANIAN JOURNAL OF FUZZY SYSTEMS

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# ***IRANIAN JOURNAL OF FUZZY SYSTEMS***

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## **Aims and Scope**

The two-monthly Iranian Journal of Fuzzy Systems (IJFS) aims to provide an international forum for refereed original research works in the theory and applications of fuzzy sets and systems in the areas of foundations, pure mathematics, artificial intelligence, control, robotics, data analysis, data mining, decision making, finance and management, information systems, operations research, pattern recognition and image processing, soft computing and uncertainty modeling.

Manuscripts submitted to the IJFS must be original unpublished works and should not be in consideration for publication elsewhere.

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